Package: cocor (via r-universe)

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Type Package **Title** Comparing Correlations Author Birk Diedenhofen [aut, cre] Maintainer Birk Diedenhofen <mail@birkdiedenhofen.de> **Depends** methods Suggests testthat Enhances rkward Imports stats **Description** Statistical tests for the comparison between two correlations based on either independent or dependent groups. Dependent correlations can either be overlapping or nonoverlapping. A web interface is available on the website http://comparingcorrelations.org. A plugin for the R GUI and IDE RKWard is included. Please install RKWard from https://rkward.kde.org to use this feature. The respective R package 'rkward' cannot be installed directly from a repository, as it is a part of RKWard. **License** GPL (>= 3) **Encoding UTF-8** LazyLoad yes URL http://comparingcorrelations.org

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Description

Statistical tests for the comparison between two correlations based on either independent or dependent groups. Dependent correlations can either be overlapping or nonoverlapping. A web interface is available on the website http://comparingcorrelations.org. A plugin for the R GUI and IDE RKWard is included. Please install RKWard from https://rkward.kde.org to use this feature. The respective R package 'rkward' cannot be installed directly from a repository, as it is a part of RKWard.

Details

The DESCRIPTION file:

Package: cocor Type: Package Version: 1.1-4 Date: 2022-06-28 Depends: methods Enhances: rkward Encoding: UTF-8 License: GPL (>= 3)

LazyLoad: yes

URL: http://comparingcorrelations.org

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See Also

Useful links:

• http://comparingcorrelations.org

aptitude

Sample dataset: aptitude

Description

Data of two samples of testees who completed an aptitude test consisting of general knowledge questions, logic tasks, and two measures of intelligence.

Usage

```
data("aptitude")
```

Format

A list that contains two data.frames holding 291 and 334 observations on the following 4 variables.

knowledge Score achieved on the general knowledge questions (numeric vector)

logic Score achieved on the logic tasks (numeric vector)

intelligence.a Intelligence measure A (numeric vector)

intelligence.b Intelligence measure B (numeric vector)

```
data("aptitude")
```

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Convert to a list of class 'htest'

Description

Convert a cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'co-cor.dep.groups.nonoverlap' to a list of class 'htest'.

Usage

```
as.htest(result.object)
## S4 method for signature 'cocor'
as.htest(result.object)
```

Arguments

result.object A cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'cocor.dep.groups.nonoverlap'.

Value

Returns a list containing a list of class 'htest' for the result of each test with the following elements:

data.name A character string giving the names of the data. estimate The two correlations that have been compared and the related correlations. A character string indicating the performed test. method null.value The specified hypothesized value of the difference between the two correlations. alternative A character string describing the alternative hypothesis. parameter The degrees of freedom of the distribution of the test statistic. statistic The value of the test statistic. p.value The p-value of the test.

The confidence interval of the difference between the two correlations.

See Also

conf.int

cocor, cocor.indep.groups, cocor.dep.groups.overlap, cocor.dep.groups.nonoverlap

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cocor	Compare two correlations based on either dependent or independent
	groups

Description

Performs a test of significance for the difference between two correlations based on either dependent or independent groups. Dependent correlations can be either overlapping (they share a variable) or nonoverlapping (they have no variable in common). The function expects raw data input from which the correlations are calculated.

Usage

```
cocor(
  formula,
  data,
  alternative = "two.sided",
  test = "all",
  na.action = getOption("na.action"),
  alpha = 0.05,
  conf.level = 0.95,
  null.value = 0,
  return.htest = FALSE
)
```

Arguments

formula	A formula specifying the correlations and their underlying variables (See details).
data	A list holding two data.frames/matrices for independent groups or a single data.frame/matrix for dependent groups that contain the variables specified in formula as columns.
alternative	A character string specifying whether the alternative hypothesis is two-sided ("two.sided"; default) or one-sided ("greater" or "less", depending on the direction). Optionally, the initial letter of the character strings ("t", "g", and "1)" can be used.
test	For the tests available, see cocor.indep.groups, cocor.dep.groups.overlap, and cocor.dep.groups.nonoverlap. Use all to apply all tests (default).
na.action	A function which handles missing data. Defaults to getOption("na.action"). See na.omit for more options.
alpha	A number defining the alpha level for the hypothesis test. The default value is .05.
conf.level	A number defining the level of confidence for the confidence interval (if a test is used that calculates confidence intervals). The default value is .95.
null.value	A number defining the hypothesized difference between the two correlations used for testing the null hypothesis. The default value is 0. If the value is other than 0, only the test zou2007 that uses a confidence interval is available.

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return.htest A logical indicating whether the result should be returned as a list containing a list of class 'htest' for each test. The default value is FALSE.

Details

Comparison of two correlations based on independent groups The formula parameter for the comparison of two correlations based on independent groups can either be ~a + b | a + b, ~a + b | a + c, or ~a + b | c + d. The variables of the first correlation – a and b before the "|" character – must refer to columns in the data.frame/matrix of the first element in the list of the data object, whereas the variables of the second correlation – a, b, c, and d after the "|" character – must refer to columns in the data.frame/matrix of the second element in the list.

Comparison of two overlapping correlations based on dependent groups The formula parameter for correlations based on dependent groups with overlapping variables must follow the pattern $\sim a + b \mid a + c$. The variables of the two correlation -a, b, and c - must refer to columns in the data frame/matrix of the data object.

Comparison of two nonoverlapping correlations based on dependent groups The formula for correlations based on dependent groups with nonoverlapping variables must have the form ~a + b | c + d. The variables of the two correlation – a, b, c, and d – must refer to columns in the data.frame/matrix of the data object.

Value

Returns an object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'cocor.dep.groups.nonoverlap' depending on the invoked comparison function.

See Also

cocor.indep.groups, cocor.dep.groups.overlap, cocor.dep.groups.nonoverlap, as.htest

```
cocor.dep.groups.nonoverlap
```

Compare two nonoverlapping correlations based on dependent groups

Description

Performs a test of significance for the difference between two correlations based on dependent groups (e.g., the same group). The two correlations are nonoverlapping, i.e., they have no variable in common. The function tests whether the correlations between j and k (r. jk) and between h and m (r.hm) differ in magnitude. Because the significance depends on the pairwise intercorrelations between all of the variables involved (j, k, h, and m), these intercorrelations have to be provided as additional parameters. The function expects correlation coefficients as input.

Usage

```
cocor.dep.groups.nonoverlap(
  r.jk,
  r.hm,
  r.jh,
  r.jm,
  r.kh,
  r.km,
  alternative = "two.sided",
  test = "all",
  alpha = 0.05,
  conf.level = 0.95,
  null.value = 0,
  data.name = NULL,
  var.labels = NULL,
  return.htest = FALSE
)
```

Arguments

r.jk	A number specifying the correlation between j and k (this correlation is used for comparison)
r.hm	A number specifying the correlation between h and m (this correlation is used for comparison)
r.jh	A number specifying the correlation between j and h
r.jm	A number specifying the correlation between j and m
r.kh	A number specifying the correlation between k and h
r.km	A number specifying the correlation between k and m
n	An integer defining the size of the group

alternative	A character string specifying whether the alternative hypothesis is two-sided ("two.sided"; default) or one-sided ("greater" or "less", depending on the direction). Optionally, the initial letter of the character strings ("t", "g", and "1)" can be used.
test	A vector of character strings specifying the tests to be used (pearson1898, dunn1969, steiger1980, raghunathan1996, silver2004, or zou2007). Use all to apply all tests (default). For further information see the tests section below.
alpha	A number defining the alpha level for the hypothesis test. The default value is .05.
conf.level	A number defining the level of confidence for the confidence interval (if test zou2007 is used). The default value is .95.
null.value	A number defining the hypothesized difference between the two correlations used for testing the null hypothesis. The default value is 0. If the value is other than 0, only the test zou2007 that uses a confidence interval is available.
data.name	A character string giving the name of the data/group.
var.labels	A vector of four character strings specifying the labels for j, k, h, and m (in this order).
return.htest	A logical indicating whether the result should be returned as a list containing a list of class 'htest' for each test. The default value is FALSE.

Value

Returns an S4 object of class 'cocor.dep.groups.nonoverlap' with the following slots:

r.jk	Input parameter
r.hm	Input parameter
r.jh	Input parameter
r.jm	Input parameter
r.kh	Input parameter
r.km	Input parameter
n	Input parameter
alternative	Input parameter
alpha	Input parameter
conf.level	Input parameter
null.value	Input parameter
data.name	Input parameter
var.labels	Input parameter

diff Difference between the two correlations, r.jk and r.hm, that were compared

For each test a slot of the same name exists with a list containing the following elements:

statistic The value of the test statistic (unless test zou2007 is used).

distribution The distribution of the test statistic (unless test zou2007 is used).

p.value The p-value of the test (unless test zou2007 is used).

conf.int The confidence interval of the difference between the two correlations (if test

zou2007 is used).

Tests

In the following, r_{jk} and r_{hm} are the two correlations that are being compared; Z_{jk} and Z_{hm} are their Z transformed equivalents. r_{jh} , r_{kh} , r_{jm} , and r_{km} are the related correlations that are also required. n specifies the size of the group the two correlations are based on. Some tests make use of Fisher's r-to-Z transformation (1921, p. 26):

$$Z = \frac{1}{2}(\ln(1+r) - \ln(1-r)).$$

pearson1898: Pearson and Filon's (1898) z

This test was proposed by Pearson and Filon (1898, p. 262, formula xl). The formula for the test statistic z is computed as

$$z = \frac{\sqrt{n(r_{jk} - r_{hm})}}{\sqrt{(1 - r_{jk}^2)^2 + (1 - r_{hm}^2)^2 - k}}$$

(Raghunathan, Rosenthal, and Rubin, 1996, p. 179, formula 1), where

$$k = (r_{jh} - r_{jk}r_{kh})(r_{km} - r_{kh}r_{hm}) + (r_{jm} - r_{jh}r_{hm})(r_{kh} - r_{jk}r_{jh})$$

$$+(r_{ih}-r_{im}r_{hm})(r_{km}-r_{ik}r_{im})+(r_{im}-r_{ik}r_{km})(r_{kh}-r_{km}r_{hm})$$

(Raghunathan et al. (1996, p. 179, formula 2). The two formulae can also be found in Steiger (1980, p. 245, formula 2 and p. 246, formula 5).

dunn1969: Dunn and Clark's (1969) z

The test statistic z of this test is calculated as

$$z = \frac{(Z_{jk} - Z_{hm})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Dunn and Clark, 1969, p. 370, formula 15), where

$$c = \left(\frac{1}{2}r_{jk}r_{hm}(r_{jh}^2 + r_{jm}^2 + r_{kh}^2 + r_{km}^2) + r_{jh}r_{km} + r_{jm}r_{kh}\right)$$

$$-(r_{jk}r_{jh}r_{jm}+r_{jk}r_{kh}r_{km}+r_{jh}r_{kh}r_{hm}+r_{jm}r_{km}r_{hm})\Big)$$

$$/((1-r_{jk}^2)(1-r_{hm}^2))$$

(Dunn and Clark, 1969, p. 368, formula 9).

steiger1980: Steiger's (1980) modification of Dunn and Clark's (1969) z using average correlations

This test was proposed by Steiger (1980) and is a modification of Dunn and Clark's (1969) z. Instead of r_{jk} and r_{hm} the mean of the two is being used. The test statistic z is given by

$$z = \frac{(Z_{jk} - Z_{hm})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Steiger, 1980, p. 247, formula 15), where

$$\bar{r} = \frac{r_{jk} + r_{hm}}{2}$$

(Steiger, 1980, p. 247) and

$$c = \frac{\frac{1}{2}\bar{r}^2(r_{jh}^2 + r_{jm}^2 + r_{kh}^2 + r_{km}^2) + r_{jh}r_{km} + r_{jm}r_{kh} - (\bar{r}r_{jh}r_{jm} + \bar{r}r_{kh}r_{km} + r_{jh}r_{kh}\bar{r} + r_{jm}r_{km}\bar{r})}{(1 - \bar{r}^2)^2}$$

(Steiger, 1980, p. 247, formula 11; in the original article, there are brackets missing around the divisor).

raghunathan1996: Raghunathan, Rosenthal, and Rubin's (1996) modification of Pearson and Filon's (1898) z

This test of Raghunathan, Rosenthal, and Rubin (1996) is based on Pearson and Filon's (1898) z. Unlike Pearson and Filon (1898), Raghunathan et al. (1996) use Z transformed correlation coefficients. The test statistic z is computed as

$$z = \sqrt{\frac{n-3}{2}} \frac{Z_{jk} - Z_{hm}}{\sqrt{1 - \frac{k}{2(1 - r_{jk}^2)(1 - r_{hm}^2)}}}$$

(Raghunathan et al., 1996, p. 179, formula 3), where

$$k = (r_{jh} - r_{jk}r_{kh})(r_{km} - r_{kh}r_{hm}) + (r_{jm} - r_{jh}r_{hm})(r_{kh} - r_{jk}r_{jh})$$
$$+ (r_{jh} - r_{jm}r_{hm})(r_{km} - r_{jk}r_{jm}) + (r_{jm} - r_{jk}r_{km})(r_{kh} - r_{km}r_{hm})$$

(Raghunathan et al., 1996, p. 179, formula 2).

silver2004: Silver, Hittner, and May's (2004) modification of Dunn and Clark's (1969) z using a backtransformed average Fisher's (1921) Z procedure

The approach to backtransform averaged Fisher's (1921) Zs was first proposed in Silver and Dunlap (1987) and was applied to the comparison of nonoverlapping correlations by Silver et al. (2004). The test is based on Steiger's (1980) approach. The formula of the test statistic z is given by

$$z = \frac{(Z_{jk} - Z_{hm})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Silver et al., 2004, p. 55, formula 5), where

$$c = \frac{\frac{1}{2}\bar{r}_z^2(r_{jh}^2 + r_{jm}^2 + r_{kh}^2 + r_{km}^2) + r_{jh}r_{km} + r_{jm}r_{kh} - (\bar{r}_zr_{jh}r_{jm} + \bar{r}_zr_{kh}r_{km} + r_{jh}r_{kh}\bar{r}_z + r_{jm}r_{km}\bar{r}_z)}{(1 - \bar{r}_z^2)^2}$$

(Silver et al., 2004, p. 56),

$$\bar{r}_z = \frac{exp(2\bar{Z} - 1)}{exp(2\bar{Z} + 1)}$$

(Silver and Dunlap, 1987, p. 146, formula 4), and

$$\bar{Z} = \frac{Z_{jk} + Z_{hm}}{2}$$

(Silver et al., 2004, p. 55).

zou2007: Zou's (2007) confidence interval

This test calculates the confidence interval of the difference between the two correlations r_{jk} and r_{hm} . If the confidence interval includes zero, the null hypothesis that the two correlations are equal must be retained. If the confidence interval does not include zero, the null hypothesis has to be rejected. A lower and upper bound for the interval (L and U, respectively) is given by

$$L = r_{jk} - r_{hm} - \sqrt{(r_{jk} - l_1)^2 + (u_2 - r_{hm})^2 - 2c(r_{jk} - l_1)(u_2 - r_{hm})}$$

and

$$U = r_{jk} - r_{hm} + \sqrt{(u_1 - r_{jk})^2 + (r_{hm} - l_2)^2 - 2c(u_1 - r_{jk})(r_{hm} - l_2)}$$

(Zou, 2007, pp. 409-410), where

$$l = \frac{exp(2l') - 1}{exp(2l') + 1},$$

$$u = \frac{exp(2u') - 1}{exp(2u') + 1}$$

(Zou, 2007, p. 406),

$$c = \left(\frac{1}{2}r_{jk}r_{hm}(r_{jh}^2 + r_{jm}^2 + r_{kh}^2 + r_{km}^2) + r_{jh}r_{km} + r_{jm}r_{kh}\right)$$

$$-(r_{jk}r_{jh}r_{jm}+r_{jk}r_{kh}r_{km}+r_{jh}r_{kh}r_{hm}+r_{jm}r_{km}r_{hm})\Big)$$

$$/((1-r_{jk}^2)(1-r_{hm}^2))$$

(Zou, 2007, p. 409), and

$$l', u' = Z \pm z_{\frac{\alpha}{2}} \sqrt{\frac{1}{n-3}}$$

(Zou, 2007, p. 406). α denotes the desired alpha level of the confidence interval.

References

Dunn, O. J., & Clark, V. A. (1969). Correlation coefficients measured on the same individuals. *Journal of the American Statistical Association*, 64, 366-377. doi:10.2307/2283746

Pearson, K., & Filon, L. N. G. (1898). Mathematical contributions to theory of evolution: IV. On the probable errors of frequency constants and on the influence of random selection and correlation. *Philosophical Transactions of the Royal Society of London, Series A*, 191, 229-311. doi:10.1098/rsta.1898.0007

Raghunathan, T. E., Rosenthal, R., & Rubin, D. B., (1996). Comparing correlated but nonoverlapping correlations. *Psychological Methods*, *1*, 178-183. doi:10.1037//1082-989X.1.2.178

Silver, N. C., & Dunlap, W. P. (1987). Averaging correlation coefficients: Should Fisher's Z transformation be used? *Journal of Applied Psychology*, 72, 146-148. doi:10.1037//0021-9010.72.1.146

Silver, N. C., Hittner, J. B., & May, K. (2004). Testing dependent correlations with nonoverlapping variables: A Monte Carlo simulation. *Journal of Experimental Education*, 73, 53-69. doi:10.3200/JEXE.71.1.53-70

Steiger, J. H. (1980). Tests for comparing elements of a correlation matrix. *Psychological Bulletin*, 87, 245-251. doi:10.1037//0033-2909.87.2.245

Zou, G. Y. (2007). Toward using confidence intervals to compare correlations. *Psychological Methods*, *12*, 399-413. doi:10.1037/1082-989X.12.4.399

See Also

cocor, cocor.indep.groups, cocor.dep.groups.overlap, as.htest

Examples

```
# Compare the difference between the correlations (age, intelligence) and
# body mass (index, shoe size) measured in the same group (all values are fictional):
r.jk <- .2  # Correlation (age, intelligence)
r.hm <- .7  # Correlation (body mass index, shoe size)
r.jh <- .4  # Correlation (age, body mass index)
r.jm <- .5  # Correlation (age, shoe size)
r.kh <- .1  # Correlation (intelligence, body mass index)
r.km <- .3  # Correlation (intelligence, shoe size)
n <- 232  # Size of the group

cocor.dep.groups.nonoverlap(r.jk, r.hm, r.jh, r.jm, r.kh, r.km, n, var.labels=c("age", "intelligence", "body mass index", "shoe size"))</pre>
```

cocor.dep.groups.overlap

Compare two overlapping correlations based on dependent groups

Description

Performs a test of significance for the difference between two correlations based on dependent groups (e.g., the same group). The two correlations are overlapping, i.e., they have one variable in common. The comparison is made between r.jk and r.jh. The function tests whether the correlations between j and k (r.jk) and between j and k (r.jh) differ in magnitude. Because the significance depends on the intercorrelation between k and k (k), this intercorrelation has to be provided as an additional parameter. The function expects correlation coefficients as input.

Usage

```
cocor.dep.groups.overlap(
    r.jk,
    r.jh,
    r.kh,
    n,
    alternative = "two.sided",
    test = "all",
    alpha = 0.05,
    conf.level = 0.95,
    null.value = 0,
    data.name = NULL,
    var.labels = NULL,
    return.htest = FALSE
)
```

Arguments

return.htest

r.jk	A number specifying the correlation between j and k (this correlation is used for comparison)
r.jh	A number specifying the correlation between j and h (this correlation is used for comparison)
r.kh	A number specifying the correlation between k and h
n	An integer defining the size of the group
alternative	A character string specifying whether the alternative hypothesis is two-sided ("two.sided"; default) or one-sided ("greater" or "less", depending on the direction). Optionally, the initial letter of the character strings ("t", "g", and "1)" can be used.
test	A vector of character strings specifying the tests to be used (pearson1898, hotelling1940, hendrickson1970, williams1959, olkin1967, dunn1969, steiger1980, meng1992, hittner2003, or zou2007). Use all to apply all tests (default). For further information see the tests section below.
alpha	A number defining the alpha level for the hypothesis test. The default value is .05.
conf.level	A number defining the level of confidence for the confidence interval (if test meng1992 or zou2007 is used). The default value is .95.
null.value	A number defining the hypothesized difference between the two correlations used for testing the null hypothesis. The default value is 0. If the value is other than 0, only the test zou2007 that uses a confidence interval is available.
data.name	A character string giving the name of the data/group.
var.labels	A vector of three character strings specifying the labels for j, k, and h (in this order).

A logical indicating whether the result should be returned as a list containing a

list of class 'htest' for each test. The default value is FALSE.

Value

Returns an S4 object of class 'cocor.dep.groups.overlap' with the following slots:

r.jk	Input parameter
r.jh	Input parameter
r.kh	Input parameter
n	Input parameter
alternative	Input parameter
alpha	Input parameter
conf.level	Input parameter
null.value	Input parameter
data.name	Input parameter
var.labels	Input parameter
4: cc	Difference between the two

Difference between the two correlations, r.jk and r.jh, that were compared diff

For each test a slot of the same name exists with a list containing the following elements:

The value of the test statistic (unless test zou2007 is used). statistic distribution The distribution of the test statistic (unless test zou2007 is used). df The degrees of freedom of the distribution of the test statistic (if test hotelling 1940,

hendrickson1970, or williams1959 is used).

p.value The p-value of the test (unless test zou2007 is used).

conf.int The confidence interval of the difference between the two correlations (if test

meng1992 or zou2007 is used).

Tests

In the following, r_{jk} and r_{jh} are the two correlations that are being compared; Z_{jk} and Z_{jh} are their Z transformed equivalents. r_{kh} is the related correlation that is additionally required. n specifies the size of the group the two correlations are based on. Some tests make use of Fisher's r-to-Ztransformation (1921, p. 26):

$$Z = \frac{1}{2}(\ln(1+r) - \ln(1-r)).$$

pearson1898: Pearson and Filon's (1898) z

This test was proposed by Pearson and Filon (1898, p. 259, formula xxxvii). The test statistic z is computed as

$$z = \frac{\sqrt{n(r_{jk} - r_{jh})}}{\sqrt{(1 - r_{jk}^2)^2 + (1 - r_{jh}^2)^2 - 2k}}$$

(Steiger, 1980, p. 246, formula 4), where

$$k = r_{kh}(1 - r_{jk}^2 - r_{jh}^2) - \frac{1}{2}(r_{jk}r_{jh})(1 - r_{jk}^2 - r_{jh}^2 - r_{kh}^2)$$

(Steiger, 1980, p. 245 formula 3).

hotelling1940: *Hotelling's* (1940) *t*

The test statistic t is given by

$$t = \frac{(r_{jk} - r_{jh})\sqrt{(n-3)(1+r_{kh})}}{\sqrt{2|R|}}$$

(Hotelling, 1940, p. 278, formula 7) with df = n - 3, where

$$|R| = 1 + 2r_{jk}r_{jh}r_{kh} - r_{jk}^2 - r_{jh}^2 - r_{kh}^2$$

(Hotelling, 1940, p. 278). The test statistic is also given in Steiger (1980, p. 246), Glass and Stanley (1984, p. 311, formula 15.7), and Hittner, May, and Silver (2003, p. 152).

williams1959: Williams' (1959) t

This test is a modification of Hotelling's (1940) t and was suggested by Williams (1959). Two mathematically different formulae for Williams' t can be found in the literature (Hittner et al., 2003, p. 152). This is the version that Hittner et al. (2003, p. 152) labeled as "standard Williams' t":

$$t = (r_{jk} - r_{jh})\sqrt{\frac{(n-1)(1+r_{kh})}{2(\frac{n-1}{n-3})|R| + \bar{r}^2(1-r_{kh})^3}}$$

with df = n - 3, where

$$\bar{r} = \frac{r_{jk} + r_{jh}}{2}$$

and

$$|R| = 1 + 2r_{jk}r_{jh}r_{kh} - r_{jk}^2 - r_{jh}^2 - r_{kh}^2.$$

An alternative formula for Williams' *t*—termed as "Williams' modified *t* per Hendrickson, Stanley, and Hills (1970)" by Hittner et al. (2003, p. 152)—is implemented in this function as hendrickson1970 (see below). The test statistic of williams1959 is also given in Steiger (1980, p. 246, formula 7) and Neill and Dunn (1975, p. 533).

Results of williams1959 are in accordance with the results of the software DEPCORR by Hittner and May (1998) and DEPCOR by Silver, Hittner, and May (2006). However, we found several typographical errors in formulae that also claim to compute Williams' t. For example, the formula reported by Boyer, Palachek, and Schucany (1983, p. 76) contains an error because the term $(1-r_{rk})$ is not being cubed. There are also typographical errors in the formula described by Hittner et al. (2003, p. 152). For example, $r_{jk} - r_{jh}$ is divided instead of being multiplied by the square root term, and in the denominator of the fraction in the square root term, there are additional parentheses so that the whole denominator is multiplied by 2. These same errors can also be found in Wilcox and Tian (2008, p. 107, formula 1).

olkin1967: Olkin's (1967) z

In the original article by Olkin (1967, p. 112) and in Hendrickson, Stanley, and Hills (1970, p. 190, formula 2), the reported formula contains a typographical error. Hendrickson and Collins (1970, p. 639) provide a corrected version. In the revised version, however, n in the enumerator is decreased by 1. This function implements the corrected formula without the decrement. The formula implemented in this function is used by Glass and Stanley (1970, p. 313, formula 14.19), Hittner et al. (2003, p. 152), and May and Hittner (1997a, p. 259; 1997b, p. 480):

$$z = \frac{(r_{jk} - r_{jh})\sqrt{n}}{\sqrt{(1 - r_{jk}^2)^2 + (1 - r_{jh}^2)^2 - 2r_{kh}^3 - (2r_{kh} - r_{jk}r_{jh})(1 - r_{kh}^2 - r_{jk}^2 - r_{jh}^2)}}.$$

dunn1969: *Dunn and Clark's* (1969) *z*

The test statistic z of this test is calculated as

$$z = \frac{(Z_{jk} - Z_{jh})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Dunn and Clark, 1969, p. 370, formula 15), where

$$c = \frac{r_{kh}(1 - r_{jk}^2 - r_{jh}^2) - \frac{1}{2}r_{jk}r_{jh}(1 - r_{jk}^2 - r_{jh}^2 - r_{kh}^2)}{(1 - r_{ik}^2)(1 - r_{jh}^2)}$$

(Dunn and Clark, 1969, p. 368, formula 8).

hendrickson1970: Hendrickson, Stanley, and Hills' (1970) modification of Williams' (1959) t

This test is a modification of Hotelling's (1940) t and was suggested by Williams (1959). Two mathematically different formulae of Williams' (1959) t can be found in the literature. hendrickson1970 is the version that Hittner et al. (2003, p. 152) labeled as "Williams' modified t per Hendrickson, Stanley, and Hills (1970)". An alternative formula termed as "standard Williams' t" by Hittner et al. (2003, p. 152) is implemented as williams1959 (see above). The hendrickson1970 formula can be found in Hendrickson, Stanley, and Hills (1970, p. 193), May and Hittner (1997a, p. 259; 1997b, p. 480), and Hittner et al. (2003, p. 152):

$$t = \frac{(r_{jk} - r_{jh})\sqrt{(n-3)(1+r_{kh})}}{\sqrt{2|R| + \frac{(r_{jk} - r_{jh})^2(1-r_{kh})^3}{4(n-1)}}}$$

with df = n - 3. A slightly changed version of this formula was provided by Dunn and Clark (1971, p. 905, formula 1.2), but seems to be erroneous, due to an error in the denominator.

steiger1980: Steiger's (1980) modification of Dunn and Clark's (1969) z using average correlations

This test was proposed by Steiger (1980) and is a modification of Dunn and Clark's (1969) z. Instead of r_{jk} and r_{jh} , the mean of the two is used. The test statistic z is defined as

$$z = \frac{(Z_{jk} - Z_{jh})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Steiger 1980, p. 247, formula 14), where

$$\bar{r} = \frac{r_{jk} + r_{jh}}{2}$$

(Steiger, 1980, p. 247) and

$$c = \frac{r_{kh}(1 - 2\bar{r}^2) - \frac{1}{2}\bar{r}^2(1 - 2\bar{r}^2 - r_{kh}^2)}{(1 - \bar{r}^2)^2}$$

(Steiger ,1980, p. 247, formula 10; in the original article, there are brackets missing around the divisor).

meng1992: Meng, Rosenthal, and Rubin's (1992) z

This test is based on the test statistic z,

$$z = (Z_{jk} - Z_{jh})\sqrt{\frac{n-3}{2(1-r_{kh})h}},$$

(Meng et al., 1992, p. 173, formula 1), where

$$h = \frac{1 - f\overline{r^2}}{1 - \overline{r^2}}$$

(Meng et al., 1992, p. 173, formula 2),

$$f = \frac{1 - r_{kh}}{2(1 - \overline{r^2})}$$

(f must be ≤ 1 ; Meng et al., 1992, p. 173, formula 3), and

$$\overline{r^2} = \frac{r_{jk}^2 + r_{jh}^2}{2}$$

(Meng et al., 1992, p. 173). This test also constructs a confidence interval of the difference between the two correlation coefficients r_{jk} and r_{jh} :

$$L, U = Z_{jk} - Z_{jk} \pm z_{\frac{\alpha}{2}} \sqrt{\frac{2(1 - r_{kh})h}{n - 3}}$$

(Meng et al., 1992, p. 173, formula 4). α denotes the desired alpha level of the confidence interval. If the confidence interval includes zero, the null hypothesis that the two correlations are equal must be retained. If zero is outside the confidence interval, the null hypothesis can be rejected.

hittner2003: Hittner, May, and Silver's (2003) modification of Dunn and Clark's (1969) z using a backtransformed average Fisher's (1921) Z procedure

The approach to backtransform averaged Fisher's (1921) Zs was first proposed by Silver and Dunlap (1987) and was applied to the comparison of overlapping correlations by Hittner et al. (2003). The test is based on Steiger's (1980) approach. The test statistic z is calculated as

$$z = \frac{(Z_{jk} - Z_{jh})\sqrt{n-3}}{\sqrt{2-2c}}$$

(Hittner et al., 2003, p. 153), where

$$c = \frac{r_{kh}(1 - 2\bar{r}_z^2) - \frac{1}{2}\bar{r}_z^2(1 - 2\bar{r}_z^2 - r_{kh}^2)}{(1 - \bar{r}_z^2)^2}$$

(Hittner et al., 2003, p. 153),

$$\bar{r}_z = \frac{exp(2\bar{Z} - 1)}{exp(2\bar{Z} + 1)}$$

(Silver and Dunlap, 1987, p. 146, formula 4), and

$$\bar{Z} = \frac{Z_{jk} + Z_{jh}}{2}$$

(Silver and Dunlap, 1987, p. 146).

zou2007: Zou's (2007) confidence interval

This test calculates the confidence interval of the difference between the two correlation coefficients r_{jk} and r_{jh} . If the confidence interval includes zero, the null hypothesis that the

two correlations are equal must be retained. If the confidence interval does not include zero, the null hypothesis has to be rejected. A lower and upper bound for the interval (L and U, respectively) is given by

$$L = r_{jk} - r_{jh} - \sqrt{(r_{jk} - l_1)^2 + (u_2 - r_{jh})^2 - 2c(r_{jk} - l_1)(u_2 - r_{jh})}$$

and

$$U = r_{jk} - r_{jh} + \sqrt{(u_1 - r_{jk})^2 + (r_{jh} - l_2)^2 - 2c(u_1 - r_{jk})(r_{jh} - l_2)}$$

(Zou, 2007, p. 409), where

$$l = \frac{exp(2l') - 1}{exp(2l') + 1},$$
$$u = \frac{exp(2u') - 1}{exp(2u') + 1}$$

(Zou, 2007, p. 406),

$$c = \frac{(r_{kh} - \frac{1}{2}r_{jk}r_{jh})(1 - r_{jk}^2 - r_{jh}^2 - r_{kh}^2) + r_{kh}^3}{(1 - r_{jk}^2)(1 - r_{jh}^2)}$$

(Zou, 2007, p. 409), and

$$l', u' = Z \pm z_{\frac{\alpha}{2}} \sqrt{\frac{1}{n-3}}$$

(Zou, 2007, p. 406). α denotes the desired alpha level of the confidence interval.

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See Also

cocor, cocor.indep.groups, cocor.dep.groups.nonoverlap, as.htest

```
# Compare the difference between the correlations (age, intelligence) and
```

^{# (}age, shoe size) measured in the same group (all values are fictional):

r.jk <- .2 # Correlation (age, intelligence)</pre>

r.jh <- .5 # Correlation (age, shoe size)

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cocor.indep.groups

Compare two correlations based on independent groups

Description

Performs a test of significance for the difference between two correlation coefficients based on independent groups. The function expects correlation coefficients as input.

Usage

```
cocor.indep.groups(
  r1.jk,
  r2.hm,
  n1,
  n2,
  alternative = "two.sided",
  test = "all",
  alpha = 0.05,
  conf.level = 0.95,
  null.value = 0,
  data.name = NULL,
  var.labels = NULL,
  return.htest = FALSE
)
```

Arguments

r1.jk	A number specifying the correlation between j and k measured in group 1
r2.hm	A number specifying the correlation between h and m measured in group 2
n1	An integer defining the size of group 1
n2	An integer defining the size of group 2
alternative	A character string specifying whether the alternative hypothesis is two-sided ("two.sided"; default) or one-sided ("greater" or "less", depending on the direction). Optionally, the initial letter of the character strings ("t", "g", and "l)" can be used.
test	A vector of character strings specifying the tests to be used (fisher1925 or zou2007). Use all to apply all tests (default). For further information see the tests section below.

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alpha	A number defining the alpha level for the hypothesis test. The default value is .05.
conf.level	A number defining the level of confidence for the confidence interval (if test zou2007 is used). The default value is .95.
null.value	A number defining the hypothesized difference between the two correlations used for testing the null hypothesis. The default value is 0. If the value is other than 0, only the test zou2007 that uses a confidence interval is available.
data.name	A vector of character strings describing the data/groups. The vector may contain one character string to describe both data sets/groups or two character strings to describe each data set/group separately.
var.labels	A vector of four character strings specifying the labels for j , k , h , and m (in this order).
return.htest	A logical indicating whether the result should be returned as a list containing a list of class 'htest' for each test. The default value is FALSE.

Value

Returns an S4 object of class 'cocor.indep.groups' with the following slots:

r1.jk	Input parameter
r2.hm	Input parameter
n1	Input parameter
n2	Input parameter
alternative	Input parameter
alpha	Input parameter
conf.level	Input parameter
null.value	Input parameter
data.name	Input parameter
var.labels	Input parameter
diff	Difference between the two correlations, r1.jk and r2.hm, that were compared

For each test a slot of the same name exists with a list containing the following elements:

statistic	The value of the test statistic (if test fisher1925 is used).
distribution	The distribution of the test statistic (if test fisher1925 is used).
p.value	The p-value of the test (if test fisher1925 is used).
conf.int	The confidence interval of the difference between the two correlations (if test zou2007 is used).

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Tests

The tests make use of Fisher's r-to-Z transformation (1921, p. 26):

$$Z = \frac{1}{2}(ln(1+r) - ln(1-r)).$$

fisher1925: Fisher's (1925) z

This significance test was first described in Fisher (1925, pp. 161-168) and its test statistic z is calculated as

$$z = \frac{Z_1 - Z_2}{\sqrt{\frac{1}{n_1 - 3} + \frac{1}{n_2 - 3}}}.$$

 Z_1 and Z_2 are the two Z transformed correlations that are being compared. n_1 and n_2 specify the size of the two groups the correlations are based on. The equation is also given for example in Peters and van Voorhis (1940, p. 188) and Cohen, Cohen, West, and Aiken (2003, p. 49, formula 2.8.11).

zou2007: Zou's (2007) confidence interval

This test calculates the confidence interval of the difference between the two correlation coefficients r_1 and r_2 . If the confidence interval includes zero, the null hypothesis that the two correlations are equal must be retained. If the confidence interval does not include zero, the null hypothesis has to be rejected. A lower and upper bound for the interval (L and U, respectively) is given by

$$L = r_1 - r_2 - \sqrt{(r_1 - l_1)^2 + (u_2 - r_2)^2}$$

and

$$U = r_1 - r_2 + \sqrt{(u_1 - r_1)^2 + (r_2 - l_2)^2}$$

(Zou, 2007, p. 409). A lower and upper bound for the confidence interval of r_1 (l_1 and u_1) and r_2 (l_2 and u_2) are calculated as

$$l = \frac{exp(2l') - 1}{exp(2l') + 1},$$

$$u = \frac{exp(2u') - 1}{exp(2u') + 1}$$

(Zou, 2007, p. 406), where

$$l', u' = Z \pm z_{\frac{\alpha}{2}} \sqrt{\frac{1}{n-3}}$$

(Zou, 2007, p. 406). α denotes the desired alpha level of the confidence interval, whereas n specifies the size of the group the correlation is based on.

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See Also

cocor, cocor.dep.groups.overlap, cocor.dep.groups.nonoverlap, as.htest

Examples

get.cocor.input

Get input parameters of a cocor result object

Description

Returns input parameters of a cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'cocor.dep.groups.nonoverlap' as a list with each slot representing a list element.

Usage

```
get.cocor.input(result.object)
## S4 method for signature 'cocor'
get.cocor.input(result.object)
```

Arguments

result.object A cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'cocor.dep.groups.nonoverlap'.

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Value

Returns a list containing all input parameters as list elements:

r1.jk	A number specifying the correlation between j and k measured in group 1 (only for result objects of class 'cocor.indep.groups').
r2.hm	A number specifying the correlation between h and m measured in group 2 (only for result objects of class 'cocor.indep.groups').
n1	An integer defining the size of group 1 (only for result objects of class 'co-cor.indep.groups').
n2	An integer defining the size of group 2 (only for result objects of class 'co-cor.indep.groups').
r.jk	A number specifying the correlation between j and k (only for result objects of class 'cocor.dep.groups.overlap' and 'cocor.dep.groups.nonoverlap').
r.jh	A number specifying the correlation between j and h (only for result objects of class 'cocor.dep.groups.overlap').
r.hm	A number specifying the correlation between h and m (only for result objects of class 'cocor.dep.groups.nonoverlap').
n	An integer defining the size of the group (only for result objects of class 'co-cor.dep.groups.overlap' and 'cocor.dep.groups.nonoverlap').
alternative	A character string specifying whether the alternative hypothesis is two-sided ("two.sided") or one-sided ("greater" or "less", depending on the direction).
alpha	A number defining the alpha level for the hypothesis test.
conf.level	A number defining the level of confidence for the confidence interval.
null.value	A number defining the hypothesized difference between the two correlations used for testing the null hypothesis.
data.name	A vector of character strings describing the data/groups.
var.labels	A vector of four character strings specifying the labels for j , k , h , and m (in this order).

See Also

get.cocor.results, cocor, cocor.indep.groups, cocor.dep.groups.overlap, cocor.dep.groups.nonoverlap

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get.cocor.results	Get result parameters of a cocor result object

Description

Returns result parameters of a cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap', or 'cocor.dep.groups.nonoverlap' as a list with each slot representing a list element.

Usage

```
get.cocor.results(result.object, test = "all")
## S4 method for signature 'cocor'
get.cocor.results(result.object, test = "all")
```

Arguments

result.object A cocor result object of class 'cocor.indep.groups', 'cocor.dep.groups.overlap',

or 'cocor.dep.groups.nonoverlap'.

test A vector of character strings specifying the tests to be returned (e.g., pearson1898,

dunn1969...). Use all to return the results of all tests (default).

Value

Returns a list containing all result parameters as list elements:

diff Difference between the two correlations that were compared.

statistic The value of the test statistic (unless test zou2007 is used).

distribution The distribution of the test statistic (unless test zou2007 is used).

df The degrees of freedom of the distribution of the test statistic (only for result ob-

jects of class 'cocor.dep.groups.overlap' if test hotelling 1940, hendrickson 1970,

or williams1959 is used).

p.value The p-value of the test (unless test zou2007 is used).

conf.int The confidence interval of the difference between the two correlations (if test

zou2007 is used).

See Also

get.cocor.input, cocor, cocor.indep.groups, cocor.dep.groups.overlap, cocor.dep.groups.nonoverlap

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